



Figure 5.9 Dimensionless recirculation time τ_{cir} and dimensionless bubble velocity $\psi = U_b/U_m$ versus Capillary number: Upper limit of Capillary number corresponds to a total superficial velocity U_m yielding a Reynolds number $Re_L = 2100$.

5.3.2.2 Absolute Recirculation Times

Now that dimensionless liquid slug recirculation times and bubble velocities are available for a set of system conditions and properties, only slug lengths are needed to compute the reference time l_s/U_b and then the absolute recirculation time from $\tau_{cir} l_s/U_b$. Liu *et al.*³⁰ proposed a dimensional correlation for slug length versus gas- and liquid-phase Reynolds numbers, and Su *et al.*³¹ reformulated this correlation to a dimensionless form as

$$\frac{l_s}{D} = 0.3694 (Re'_L)^{0.585} Re_G^{-0.483}. \tag{5.14}$$

where Re'_L and Re_G are Reynolds numbers of the gas and liquid phases based on tube diameter and the respective superficial velocities:

$$Re'_L = \frac{U_{Ls} D}{\nu_L}, \quad Re_G = \frac{U_{GS} D}{\nu_G}. \tag{5.15}$$

For superficial liquid velocities corresponding to slug-flow crystallizers seeded by upstream coaxial and radial mixers by Jiang *et al.*,² the absolute slug length is plotted versus superficial gas velocity in Figure 5.10. For the actual values of the superficial gas velocity U_{GS} used in the two experiments, the measured and calculated liquid slug lengths are given in Table 5.1. Eqn